

Lindsay went to her doctor to get a new prescription for toenail fungus. Her doctor talked to her about the importance of taking her medicine regularly. When explaining this new medication to Lindsay, he used the following half-life function, where t represents time in hours:

$$M(t) = 60 \left(\frac{1}{2} \right)^{\frac{t}{12}}$$

Explain what each part of the equation would represent.

Initial amount of medication = 60 units ; This would represent the beginning amount of medication that the doctor gives Lindsay. We know this because the value of 60 is in the spot where a would go in the standard half-life formula $y = a \left(\frac{1}{2} \right)^{\frac{t}{h}}$, and a is the y-intercept/starting value of the equation.

Length of half-life cycles = 12 hours ; This would represent the length of the half-life cycles because we know that time is t and we have to divide the exponent of time t by the length of the half-life cycles to end up with the number of half-life cycles.

Amount of medicine present after t hours = $M(t)$ units ; This would represent the amount of medicine present after t hours. We know this because it is the ending amount of the equation using function notation (same as $y =$ in the standard formula).

Additional Practice:

The half-life of a foul substance is 4 years. If you have 8oz. of this strange substance, how much will be left in 20 years?

$$y = a(b)^{\frac{t}{h}}$$

Identify the values that each variable in the equation would represent and explain how you know.

1. $a =$
2. $b =$
3. $t =$
4. $h =$

When you solve for y , what are you finding?

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$$M(t) = 60 \left(\frac{1}{2}\right)^{\frac{t}{12}}$$

Explain what each part of the equation would represent.

60 = initial amount of medicine ; We know this because the value of 60 is in the spot where **a** would go in the standard half-life formula $y = a \left(\frac{1}{2}\right)^{\frac{t}{h}}$, and **a** is the y-intercept/starting value of the equation.

1/2 = decay factor (half-life) ; This would represent the decay factor **b** in the standard exponential formula $y = a(b)^x$. Because the medication has a decay factor of $\frac{1}{2}$ or 50%, we know that **b** has to be $\frac{1}{2}$.

t = time in hours ; This would represent the time in hours because it is the variable in the exponent.

12 = length of the half-life cycle ; This would represent the length of the half-life cycles because we know that time is **t** and we have to divide the exponent of time **t** by the length of the half-life cycles to end up with the number of half-life cycles.

M(t) = amount of medicine present after **t** hours ; This would represent the amount of medication after **t** hours because it is the ending amount of the equation using function notation (same as $y =$ in the standard formula).

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