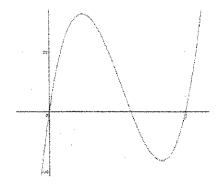
I can represent cubic functions using words, tables, graphs & equations. I can determine domain and range of cubic functions in context. I can connect characteristics to factors. (C2, C3)

1. The volume V(x) of a box is defined by the function: V(x) = x(6-2x)(10-2x), where each factor represents a dimension of the box. What is the domain and range of the function? What is the domain and range in context?



a) Function (theoretical):

Domain: $\mathbb{R}(-\infty,\infty)$

Range: $\mathbb{R}(-\infty, \infty)$

b) Context (practical):

Domain: (0,3)

Range: (0, 32.835) - approx.

c) What do the practical domain and range mean for this problem? Practical Domain represent lengths possible to cut from the corner of the paper to create heights for the box. Practical Runge represents possible Volumes the you could have.

I can determine if a graph or an equation represents an even or odd function. (C4)

2. Evaluate for the criteria that apply determine whether each is an even or odd function.

i)

a) $f(x) = 5x^4 - 7x^2 + 9$

-on voriables

Describe the exponents: We ever

ii) $f(-x) = 5(-x)^{4} - 7(-x)^{2} + 9$ = $5x^{4} - 7x^{2} + 9 = f(x)$

iii) Is the function odd, even, or neither?

rsyen

on variables b) $h(x) = ax^7 - bx^5 + cx^3 - 9$

Describe the exponents: mixture of odd/even

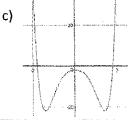
ii)

 $f(-x) = \alpha(-x)^{7} - b(-x)^{5} + c(-x)^{3} - q$ $= -\alpha x^{7} + bx^{5} - cx^{3} - q + f(x) + -f(x)$ Is the function odd, even, or neither?

iii)

What type (if any) of symmetry does it have?

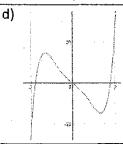
- ii) f(-x) = f(x)
- iii) Is the function odd, even, or neither?



What type (if any) of symmetry does it have?

000

- ii) f(-x) = -f(x)
- iii) Is the function odd, even, or neither?



I can determine the possible number of relative extrema, number absolute extrema, the number of possible zeros by looking at the degree of a polynomial. (C5)

- 3. State the number(s) of possible relative extrema, number of absolute extrema & possible number(s) of zeros for each
- (a) f(x) is a 5th degree polynomial:

Relative 4,2, or 0 Absolute 0 Zeros 5

(b) f(x) is a 6th degree polynomial:

Relative 5,3,1 Absolute ____ Zeros ____ &

I can find extrema, intervals of increase or decrease, end behaviors, and possible number of zeros based on the degree of the polynomial. (C6)

4.
$$f(x) = (x+3)^2(x+2)$$

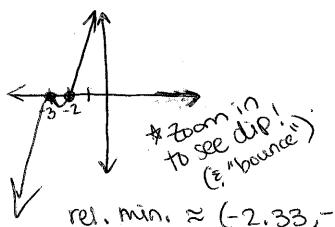
Number of Absolute Extrema:

Number of Relative Extrema:

Intervals of Increase: $(-\infty, -3)U(-2.33, \infty)$

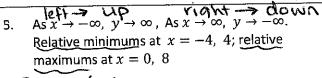
Intervals of Decrease: (-3, -2.33)

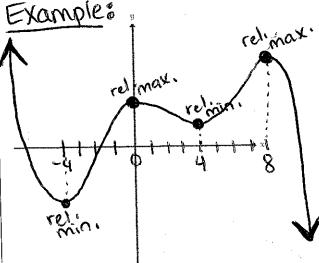
End Behavior: As $x \to -\infty$, $y \to -\infty$, As $x \to \infty$, $y \to -\infty$



rel. min. ≈ (-2.33,-0.15)

I can draw a graph of a polynomial function given the characteristics. (C7)





Answers will vary for y-values of max/min Points, but X-values & behavior/shape

Should be the same

6. Roots: x = -4, -1 with multiplicity 2, 3 with multiplicity 3. Absolute maximum at x = 1

Example: obs. max, roots on X-axis

Answers will vary for Y-value of ows. max

point, but X-values E behavior/shape Should be the same

I can understand the fundamental theorem of algebra. (C8)

Circle all that are possible.

- 7. Quartic Function (degree 4)
- (a) 1 real root, 4 imaginary roots
- (b) 3 real roots; 1 imaginary root
- (c))4 real roots, 0 imaginary roots
- (d) 2 real roots, 2 imaginary roots
- (e) 5 real roots, 0 imaginary roots

- 8. Quintic Function
- (degree 5)
- (a) 7 real roots, 0 imaginary roots
- (b) 🕽 real roots, 2 imaginary roots
- (c) 4 real roots, 1 imaginary root
- (d) I real root, 4 imaginary roots
 - (e) 2 real roots, 3 imaginary roots

I can write polynomials in standard and factored form and find their zeros. (C9, C10)

9. Write in standard form:

$$(4x+1)^{2}(3-x)$$

$$(4x+1)(4x+1)(3-x)$$

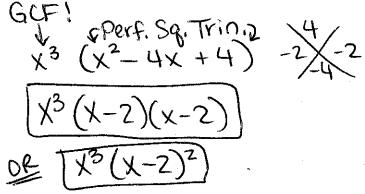
$$1(6x^{2}+4x+4x+1)$$

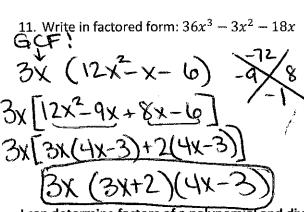
$$(16x^{2}+8x+1)(3-x)$$

$$18x^{2}-1(6x^{3}+24x-8x^{2}+3-x)$$

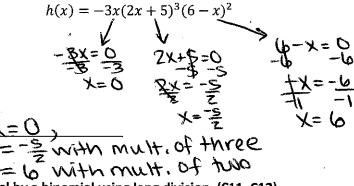
$$-1(6x^{3}+40x^{2}+23x+3)$$

10. Write in factored form: $x^5 - 4x^4 + 4x^3$



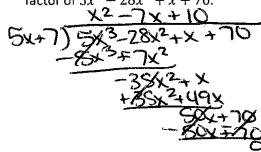


12. Find the zeros algebraically and indicate multiplicity:



I can determine factors of a polynomial and divide a polynomial by a binomial using long division. (C11, C12)

13. Use long division to determine if 5x + 7 is a factor of $5x^3 - 28x^2 + x + 70$.



14. Use long division to evaluate

$$4x^{4} - 19x^{3} + 24x^{2} - 49x - 10 \div 4x - 3.$$

$$x^{3} - 4x^{2} + 3x - 10$$

$$-4x^{4} + 3x^{3} + 24x^{2} - 49x - 10$$

$$-4x^{4} + 3x^{3}$$

$$-16x^{3} + 24x^{2}$$

$$-19x^{3} + 24x^{2}$$

Is 5x + 7 a factor of $5x^3 - 28x^2 + x + 70$?

Yes, blc R=0,

I can divide a polynomial by a binomial using synthetic division. I can write the dividend as the product of the divisor and the quotient plus the remainder. (C13)

15. Use synthetic division to determine if x-3 is a factor of $3x^4 - 2x^2 - 70x - 20$.

Is
$$x - 3$$
 a factor of $3x^4 - 2x^2 - 70x - 20$?

17. Use your answer in #15 to write the polynomial as a product of the divisor and the quotient plus the remainder.

$$2x^4 + 16x^3 + 34x^2 - 4x + 48 \div x + 4$$
.

$$\frac{-412}{\sqrt{-8}} = \frac{10}{34} = \frac{34}{-4} = \frac{48}{48}$$

$$\frac{1}{2} = \frac{8}{32} = \frac{-8}{2} = \frac{48}{12}$$

$$2x^3 + 8x^2 + 2x - 12, R96$$

$$3x^4 - 2x^2 - 70x - 20 = (x-3)(3x^3 + 9x^2 + 25x + 5) + -5$$

I can use the remainder theorem to evaluate a polynomial for a given value. I can use the remainder theorem to find a missing value. (C14)

18. Given
$$\frac{P(x)}{x-4} = x^2 - 5x + 6R42$$
 what is $P(4)$?

Show work or explain your answer.

Since +4 is the root of the divisor x-4, the Remainder Thm. says that P(4) = Remainder, 16+8+2a+4=34

So
$$P(4)=42$$

19. If
$$\frac{x^4 + 2x^2 + ax + 4}{x - 2} = x^3 + 2x^2 + 6x + 15 R 34$$
,

solve for a. Show your work.

$$(2)^{4}+2(2)^{2}+\alpha(2)+4=34$$

 $10+8+2\alpha+4=34$

$$28 + 2a = 34$$

 -28

I can divide polynomials and factor completely. (C15)
$$\frac{L\alpha}{\alpha} = \frac{L\alpha}{\alpha} = \frac{L\alpha}{\alpha}$$

can divide polynomials and factor completely. (C15)
$$20. \text{ Given } 2x + 3 \text{ is a factor of } h(x), \text{ factor } h(x) = 10x^4 + 23x^3 - 12x^2 - 36x \text{ completely.}$$

$$\begin{array}{r}
5x^3 + 4x^2 - 12x \\
2x + 3) 10x^4 + 23x^3 - 12x^2 - 36x \\
-10x^4 + 15x^3 \\
8x^3 - 12x^2 \\
-24x^2 - 36x \\
+24x^2 + 36x
\end{array}$$

/ put back with priginal factor

GCF!
$$\times (5x^2+4x-12)$$
 $\times (5x^2+10x-6x-12)$ $\times (5x^2+10x-6x-12)$ $\times (5x^2+10x-6x-12)$

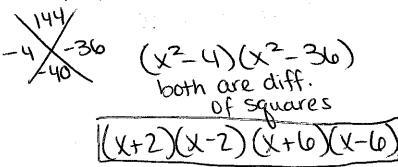
I can factor higher order polynomials using grouping and by using quadratic form. (C16)

21. Factor completely. $x^3 - 3x^2 - 16x + 48$

pletely.
$$x^3 - 3x^2 - 16x + 48$$

 $x^2(x-3) - 16(x-3)$
 $(x-3)(x^2 - 16)$
 $x^3 - 3x^2 - 16x + 48$
 $(x-3)(x-3)(x-16)$
 $x^3 - 3x^2 - 16x + 48$

22. Factor completely. $x^4 - 40x^2 + 144$



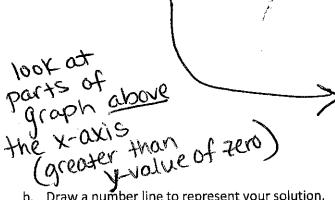
I can factor a sum of cubes and a difference of cubes. (C17)

23. Write in factored form: $8x^3 + 27$

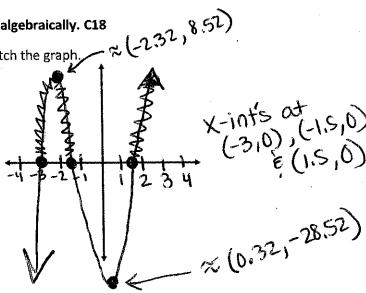
sum of cubes 2x+3)(4x2-6x+9) 24. Write in factored form: $125w^3 - 64$

I can find the solution to a polynomial inequality graphically and algebraically. C18

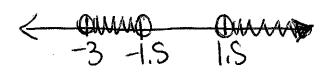
25. Solve by factoring and sketching: $4x^3 + 12x^2 - 9x - 27 > 0$



a. Sketch the graph,



- Draw a number line to represent your solution.
- Write your solution in interval notation.



$$(-3,-1.5)$$
 $U(1.5,\infty)$

*open circles on x-values

I can find the solution to a polynomial inequality graphically. I can represent a solution to a polynomial inequality using inequalities, interval notation, number lines, and verbal descriptions in context. C19

Emilio has been trying to regulate the pH level in his aquarium for 5 hours. For the water to be safe for the fish, he must keep the pH less than or equal to 9. The function $p(x) = -0.34x^3 + 2.652x^2 - 5.4638x + 11.1114$ represents the pH level in the tank x hours since Emilio began to regulate it.

- 26. Write and solve an inequality to determine the time intervals during which the pH was safe for Emilio's fish. State your solution in interval notation. Explain in words what your solution means. Sketch the graph.
- a. Write and solve an inequality to determine the time intervals during which the pH was safe for Emilio's fish.

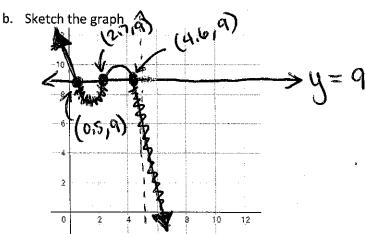
 $-0.34x^3 + 2.652x^2 - 5.4638x + 11.1114 \le 9$

Solution: 0,5≤ X ≤ 2.7 (approx.): or 4.6 ≤ X ≤ 5

c. State your solution in interval notation.

[0,5,2.7] U [4.6,5]

requising for 5 hours



d. Explain in words what your solution means.

Emilio's aquariums

PH value is safe for fish

between 0,5 & 2.7 hours

and from 4.6 hours

up to the 5th hour

that he was trying to

regulate