Math 3 - Equation of a Circle (CP)

To the right is a circle graphed on a coordinate grid. Through the next series of questions, we will develop the **equation of circle** used to graph a circle on a coordinate grid.

The definition of a **circle** is a set of points equidistant from a fixed point.

(1) The fixed point is called the ______ of the circle. In the figure to the right, label this point C(h, k).

(2) Pick a point anywhere on the boundary of the circle and label it P(x, y).

(3) The distance between the center and any point on the circle is called the ______. Draw a segment from the point C to point P and label it *r*.

(4) Use the Pythagorean Theorem to solve for r^2 .



The equation in question 4 is the equation of a circle with center ______ and radius ______.

EXAMPLES

(A) Identify the center and radius of the circle and then graph on the coordinate grid provided.

 $(x-3)^2 + (y-2)^2 = 9$



(B) Determine the center and radius of the circle graphed to the right and write the equation.

$$x^2 + (y + 3)^2 = 4$$





(1) Match the equation of a circle with its description.

 $x^2 + y^2 = 4$ A. center: (-1, 4); radius: 4 I. II. $x^2 + y^2 = 9$ B. center: (-2, -3); radius: 3 III. $(x + 1)^2 + (y - 4)^2 = 16$ C. center: (0, 0); radius: 2 IV. $(x + 2)^2 + (y + 3)^2 = 9$ D. center: (2, 5); radius: 3 V. $(x + 3)^2 + (y - 5)^2 = 16$ E. center: (-3, 5); radius: 4 VI. $(x-2)^2 + (y-5)^2 = 9$ F. center: (0, 0); radius: 3 (2) Write the equation of each circle described below. (a) center: (2, 4); radius: 5 (b) center: (4, -1); radius: 6

(3) Identify the center and radius of the circle and then graph on the coordinate grid provided.



(4) Determine the equation of each circle graphed below.

(b)



(a)

(c) center: (0, 5); radius: 3.2





(d) center: (-9, 0); radius: 10

