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1. A circle of radius $r$ has a center at point ( $h, k$ ) and includes the point ( $x, y$ ). Find the distance from the point $(h, k)$ to the point ( $x, y$ ). Then explain how this equation relates to the equation of a circle. A picture may be helpful.


| $d=\sqrt{\left(x_{2}-x_{1}\right)^{2}+\left(y_{2}-y_{1}\right)^{2}}$ | First I substituted the coordinates of my <br> points into the distance formula. This gave <br> me the length of $r$, which is the radius of <br> the circle drawn. |
| :---: | :--- |
| $r=\sqrt{(x-h)^{2}+(y-k)^{2}}$ | $r^{2}=(x-h)^{2}+(y-k)^{2}$ |
| Then I squared both sides of the equation. <br> That gave me the standard form of an <br> equation of a circle with a center at $(h, k)$ <br> and a radius of $r$. |  |

2. Write the equation for a circle with a center at $(-3,2)$ and a radius of 4.

| $(x-h)^{2}+(y-k)^{2}=r^{2}$ | ALWAYS write down the formula or equation. |
| :---: | :--- |
| $(x--3)^{2}+(y-2)^{2}=4^{2}$ | Then substitute the given information into the equation. <br> $(\mathrm{h}=-3, \mathrm{k}=2, \mathrm{r}=4)$ |
| $(x+3)^{2}+(y-2)^{2}=16$ | Then simplify where possible. |

3. Identify the center and radius for the following circle. $\quad(x-5)^{2}+(y+4)^{2}=50$

I am comparing the given equation with the standard equation:

$$
(x-h)^{2}+(y-k)^{2}=r^{2}
$$

When I do this, I have to remember that the minus sign is part of the standard equation. That means in $(x-5)^{2}$, the h-value is 5 . In $(y+4)^{2}$, I have to think of it as $(y-4)^{2}$ to understand why the $k$-value is -4 . So the center is $(5,-4)$. The radius is found by square rooting $r^{2}$. Here that means the radius would be $\sqrt{50}$. I can simplify this answer by factoring 50 into $25 \cdot 2$. Then $\sqrt{50}=\sqrt{25 \cdot 2}=\sqrt{25} \cdot \sqrt{2}$ or $5 \sqrt{2}$.

Additional Practice:

1. Write an equation in standard form for a circle with a center at $(3,5)$ and a radius of 6 .
2. Now write an equation in standard form for a circle with a center at $(-3,5)$ and a radius of 6 .
3. What did you have to change in the equation when the center was at -3 instead of 3 ?
4. Find the center and radius of the circle formed by the equation: $(x-2)^{2}+(y-3)^{2}=9$
5. Find the center and radius of the circle formed by the equation: $(x+4)^{2}+(y+2)^{2}=9$
6. Find the center and radius of the circle formed by the equation: $(x-2)^{2}+(y+3)^{2}=2$
