PCFU CP: Completing the Square to Find the Center and Radius D2 & D3

Find the center and radius of the circle below. Show all work.

$$x^2 + y^2 - 3x - 10y - 13 = 0$$

1. The first thing I needed to do was to move the constant, -13, so I added 13 to both sides.

2. Then I rearranged my terms so that the x-terms and the y-terms were grouped together.

3. The coefficient on the squared terms is 1 so I did not have to divide before I could complete the square.

4. Next I needed to figure out what should be added to the x-terms to make a perfect square trinomial. (I will add the same number on the other side to keep the equation balanced.) I knew that the -3x came from two identical terms being combined so I divided -3 by 2 which gave me $\frac{-3}{2}$ or -1.5. I then squared this to determine what I needed to add. $\left(\frac{-3}{2}\right)^2 = \frac{9}{4}$ or 2.25.

5. After that I completed the square on the y-terms to make a perfect square trinomial. In this case I knew two identical terms were combined to give me -10y. I divided -10 by 2 to get -5. I then squared -5 to determine what I needed to add to both sides. $(-5)^2$ =25 so I added 25 to both sides of my equation.

6. At this point it was time for me to factor my perfect square trinomials I created and to "clean up" the numbers on the right side of my equation.

7. At last I compared my equation with the standard form equation of a circle:

$$(x-h)^2 + (y-k)^2 = r^2$$

Self-Assessment

I understood I needed to complete the square in order to convert the equation to standard form.YesNoI correctly completed the square to convert the equation to standard form.YesNoI correctly factored the perfect square trinomials.YesNoI correctly identified the center from my equation in standard form.YesNo	I correctly reordered the equation to group the x and y values together.	Yes	No
I correctly completed the square to convert the equation to standard form.YesNoI correctly factored the perfect square trinomials.YesNoI correctly identified the center from my equation in standard form.YesNo	I correctly isolated the constant on the other side of the equation.	Yes	No
I correctly factored the perfect square trinomials. Yes No I correctly identified the center from my equation in standard form. Yes No	I understood I needed to complete the square in order to convert the equation to standard form.	Yes	No
I correctly identified the center from my equation in standard form. Yes No	I correctly completed the square to convert the equation to standard form.	Yes	No
	I correctly factored the perfect square trinomials.	Yes	No
	I correctly identified the center from my equation in standard form.	Yes	No
I correctly identified the radius from my equation in standard form. Yes No	I correctly identified the radius from my equation in standard form.	Yes	No

Additional Practice

- 1. Complete the square for each of the following:
 - a) $x^2 + 16x +$ ____ b) $y^2 2y +$ ____

c)
$$x^2 + 7x + __$$
 d) $y^2 + 9y + __$

1. $x^{2} + y^{2} - 3x - 10y - 13 + 13 = 0 + 13$ 2. $x^{2} - 3x + y^{2} - 10y = 13$ 3. $(x^{2} - 3x + _) + y^{2} - 10y = 13 + _$

4.
$$(x^2 - 3x + 2.25) + y^2 - 10y = 13 + 2.25$$

5.
$$(x^2 - 3x + 2.25) + (y^2 - 10y + _) = 13 + 2.25 + _$$

 $(x^2 - 3x + 2.25) + (y^2 - 10y + 25) = 13 + 2.25 + 25$

6.
$$(x - 1.5)^2 + (y - 5)^2 = 40.25$$

7. The center is (1.5, 5) and the radius is $\sqrt{40.25} \approx 6.34$.

2. Factor each as a perfect square:

a)
$$x^{2} - 8x + 16$$

b) $x^{2} + 18x + 81$
c) $y^{2} + 24y + 144$
d) $y^{2} - 14y + 49$
e) $x^{2} + 5x + 6.25 \text{ or } x^{2} + 5x + \frac{25}{4}$
f) $y^{2} - 7y + \frac{49}{4} \text{ or } y^{2} - 7y + 12.25$

3. Identify the center and radius of each circle:

a)
$$(x - 8)^2 + (y - 7)^2 = 81$$

Center: Radius: r=
b) $(x + 8)^2 + (y + 7)^2 = 36$
Center: Radius: r=
c) $(x - 8)^2 + (y + 7)^2 = 20$
Center: Radius: r=
d) $\left(x + \frac{1}{2}\right)^2 + \left(y - \frac{7}{4}\right)^2 = \frac{25}{4}$
Center: Radius: r=

4. Now put it all together. Complete the square; write in factored form; and then identify the center and radius of $x^2 + y^2 + 18x - 9y - 19.75$. Show all steps.